UNIVERSITY OF CRAIOVA Faculty of Mathematics and Informatics Fundamental domain : MATHEMATICS Speciality : MATHEMATICS Duration of studies : 3 years

Arithmetic in rings

Instructor : Lector.dr. Christina-Theresia Dan

Cod: M2406 Cycle I: LICENCE Second Year, Semester IV, Cours 28 hours, Seminar 28 hours Nr. of credits: 5 Domain: Mathematics Type : optional Category : specialized discipline Objectives: To have a knowledge of the principal types of rings: euclidean, principal, factorial:

definitions, fundamental properties and characteristic computing algorithms; to apply the basic results of arithmetics in rings in solving applicative problems.

Necessary background: The courses of: logics and set theory, algebra (I, II).

Evaluation form : Colocutional examination (C)

Contents:

C ₁ :	The relation of divisibility. Association in divisibility.
C ₂ :	The greatest common divisor. The least common multiple.
C ₃ :	Irreducible elements. Prime elements.
C ₄ :	Euclidean rings.
C ₅ :	Bézout's relations.
C ₆ :	Linear equations in euclidean rings.
C ₇ :	Principal rings.
C ₈ :	Factorization in principal rings.
C ₉ :	Factorial rings.
$C_{10} - C_{11}$:	The factoriality of the polinomial rings.
C ₁₂ :	Criteria for irreducible polinoms.
$C_{13} - C_{14}$:	Factorization of polinoms with integer coefficients: Berlekamp's algorithm;
	modular factorization for polynoms from $\mathbb{Z}[X]$.

Bibliography:

- 1. Albu, T., Ion, I. D., *Itinerar elementar în algebra superioară*, Editura All Educational, București, 1997.
- 2. Bușneag, D., Capitole speciale de algebră, Editura Universitaria, Craiova, 1997.
- 3. Dincă, Al., Dan, C., Algebră III, Editura Universitaria, Craiova, 2009.
- 4. Ion, I. D., Radu, N., Algebră, Editura Didactică și Pedagogică, București, 1981.
- 5. Năstăsescu, C., Niță, C., Bazele algebrei I, Editura Academiei, București, 1986.