

**UNIVERSITY OF CRAIOVA**  
**Faculty of Mathematics and Informatics**  
**Department of Mathematics**  
**Fundamental domain : MATHEMATICS**  
**Master 2: APPLIED MATHEMATICS**  
**Duration of studies : 2 years**

Approved with academic year  
2008-2009

### *Elements of cryptography*

Instructor : Lector dr. Christina-Theresia Dan

**Cod:** MA 223

**Cycle II:** Master

Second Year , Semester IV, Cours 28 hours, Seminar 28 hours

**Nr. of credits:** 6

**Domain:** Mathematics

**Type :** fundamental

**Category :** specialized discipline

**Objectives:** To have a knowledge of the basic notions and principles of cryptology; to know the major cryptosystems with secret key, DES and AES; to study the most popular public-key cryptosystems and their security; to apply mathematical notions in solving applicative problems.

**Necessary background:** The courses of: elementary number theory, algorithms in number theory, algebra (I, II and III), computer programming.

**Evaluation form :** Exam (E)

#### **Contents:**

- C<sub>1</sub> :** *Basic notions.* Information security and cryptography. Basic concepts. Brief history of cryptography.
- C<sub>2</sub> :** *Special classes of functions:* One way functions, trapdoor, hash. *Detecting error and methods of correction.* Generating random numbers.
- C<sub>3</sub> :** *Symmetric-key encryption.* Substitution ciphers: monoalphabetic (Cezar, affine), polyalphabetic (Vigenere, Playfair, Hill). Cryptanalysis of such ciphers.
- C<sub>4</sub> :** *Data Encryption Standard (DES).* Product ciphers. Feistel cipher. Description of the cryptographic scheme DES. Utility of DES. Cryptosystems related with DES.
- C<sub>5</sub> :** *Various attacks on DES.* Meet in the middle, differential and linear cryptanalysis.
- C<sub>6</sub> :** *Advanced Encryption Standard (AES).* History. Description of the finalist cryptosystems for AES (Mars, RC6, Serpent, Twofish). AES.
- C<sub>7</sub> :** *Public-key cryptography.* Basic notions. The security of secret-key cryptosystems. Symmetric-key vs public-key cryptography.
- C<sub>8</sub> :** *RSA public-key cryptosystem.* Description. Implementation. RSA encryption in practice.
- C<sub>9</sub> :** *Security of RSA.* Relation to factoring. Small encryption exponent  $e$ . Message concealing. Another attacks.
- C<sub>10</sub> :** *El Gamal public-key cryptosystem.* Description. Security of discrete logarithms. Generalized El Gamal encryption.

- C<sub>11</sub>: *Knapsack public-key encryption*. Merkle-Hellman encryption. Chor-Rivest public-key encryption.
- C<sub>12</sub> - C<sub>13</sub>: *Digital signature*. Introduction. Basic notions. A classification of digital signature schemes and short presentation. Types of attacks on signature scheme. *RSA* signature and possible attacks. El Gamal signature. Digital standard signature (*DSS*).
- C<sub>14</sub>: *Data base security and secret sharing*.

**Bibliography:**

1. Buşneag, D., Boboc, F., Piciu, D., *Aritmetică și teoria numerelor*, Editura Universitaria, Craiova, 1999.
2. Dan, C., *Algoritmi în teoria numerelor*, Editura Universitaria, Craiova, 2005.
3. Koblitz, N., *A Course in Number Theory and Cryptography*, ed. a II-a, Springer-Verlag, Berlin, 1994.
4. Knut, D.E., *The Art of Computer Programming*, vol. I, ed. a II-a, Addison-Wesley, 1973.
5. Menezes, A., Oorschot, P., Vanstone, S., *Handbook of Applied Cryptography*, CRC Press, Boca Raton, Florida, 1998.
6. Yan, Song Y., *Number theory for computing*, ed. a II-a, Springer Verlag, 2002.